MATHEMATICS



DPP No. 41

Topics: Sequence & Series, Application of Derivatives

Type of Questions M.M., Min.

Comprehension (no negative marking) Q.1 to Q.3 Single choice Objective (no negative marking) Q. 4,5 Fill in the Blanks (no negative marking) Q.6

(3 marks, 3 min.) 91 (3 marks, 3 min.) 6]

Subjective Questions (no negative marking) Q.7,8

(4 marks, 4 min.) 4] 101 (4 marks, 5 min.)

COMPREHENSION (Q. NO. 1 TO 3)

Consider
$$S_n = \frac{8}{5} + \frac{16}{65} + \dots + \frac{8r}{4r^4 + 1}$$

1. Sum of infinite terms of above series will be

- (A) 0
- (B) 1/2
- (C)2
- (D) None of these

2. The value of S₁₆ must be

- (A) $\frac{80}{41}$
- (B) $\frac{1088}{545}$
- (C) $\frac{107}{245}$
- (D) None of these

If $S_n = \frac{an^2 + bn}{cn^3 + dn^2 + en + 1}$, where a, b, c, d, e are independent of 'n', then 3.

- (A) a = 4, e = 2
- (B) c = 0, d = 4 (C) b = 4, e = 4
- (D) None of these

Tangent and normal to the curve y = 2 sinx + sin2x are drawn at p $\left(x = \frac{\pi}{3}\right)$. The area of the quadrilateral 4.

formed by the tangent, the normal and coordinate axes is.

- (A) $\frac{\pi\sqrt{3}}{2}$
- (B) $\frac{\pi}{2}$
- (C) $\frac{\sqrt{3}}{2}$
- (D) None of these

The point(s) of minimum of the function, $f(x) = 4x^3 - x |x-2|$, $x \in [0, 3]$ is : 5.

The value of a for which the function $f(x) = (4a - 3)(x + \log 5) + 2(a - 7) \cot \frac{x}{2} \sin^2 \frac{x}{2}$ does not 6.

posses critical points is

7. Find the difference between the greatest and least values of the function,

$$f(x) = \cos x + \frac{1}{2} \cos 2x - \frac{1}{3} \cos 3x.$$

Find values of a and b such that $f(x) = \frac{a}{x} + bx$ has a minimum at point (1, 6). 8.





Answers Key

1. (C) **2.** (B) **3.** (A) **4.** (A)

5. (B) **6.** $(-\infty, -4/3) \cup (2, \infty)$

7. 9/4 8. a = b = 3

